

# A recurrence-based technique for detecting genuine extremes in instrumental temperature records

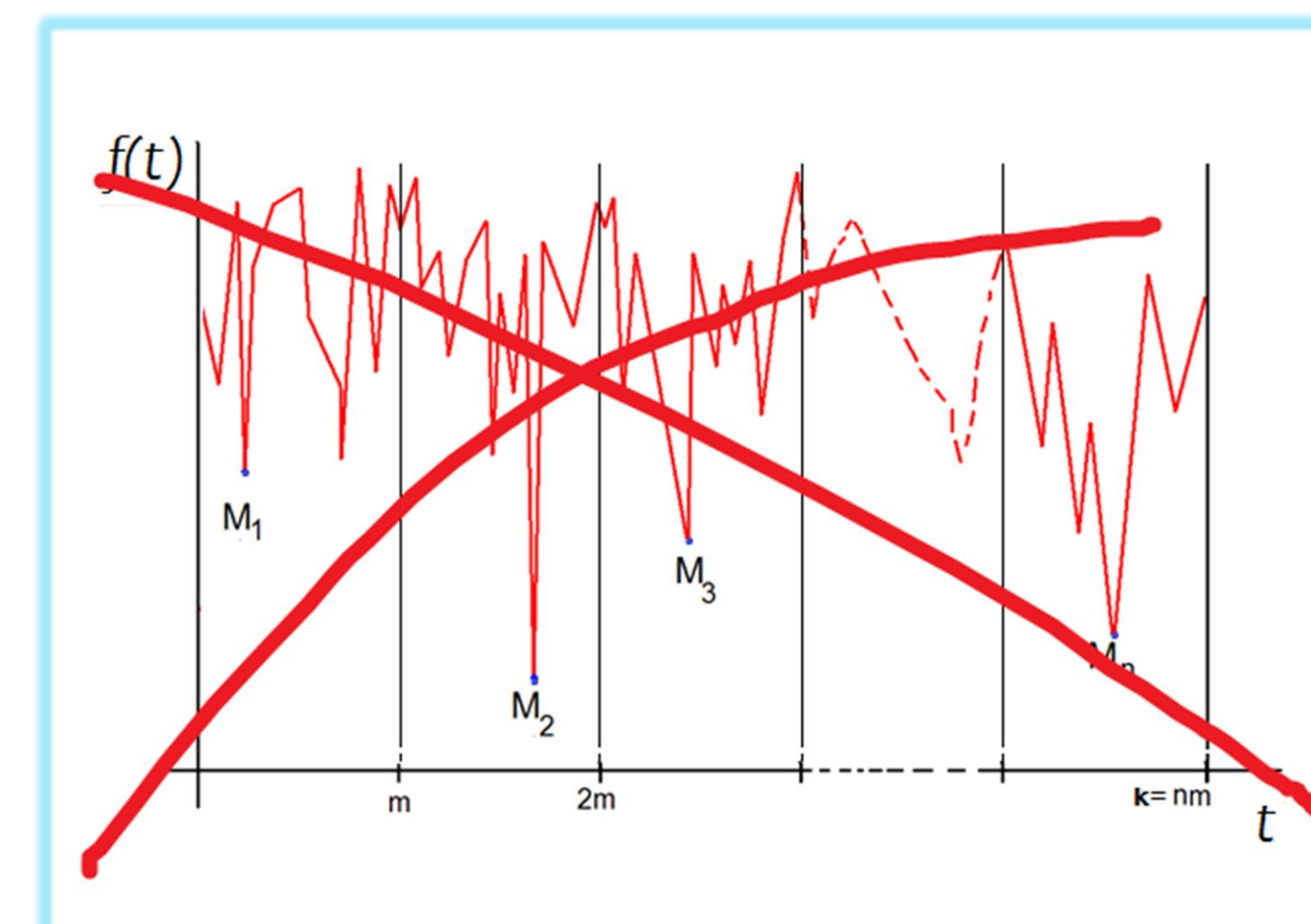
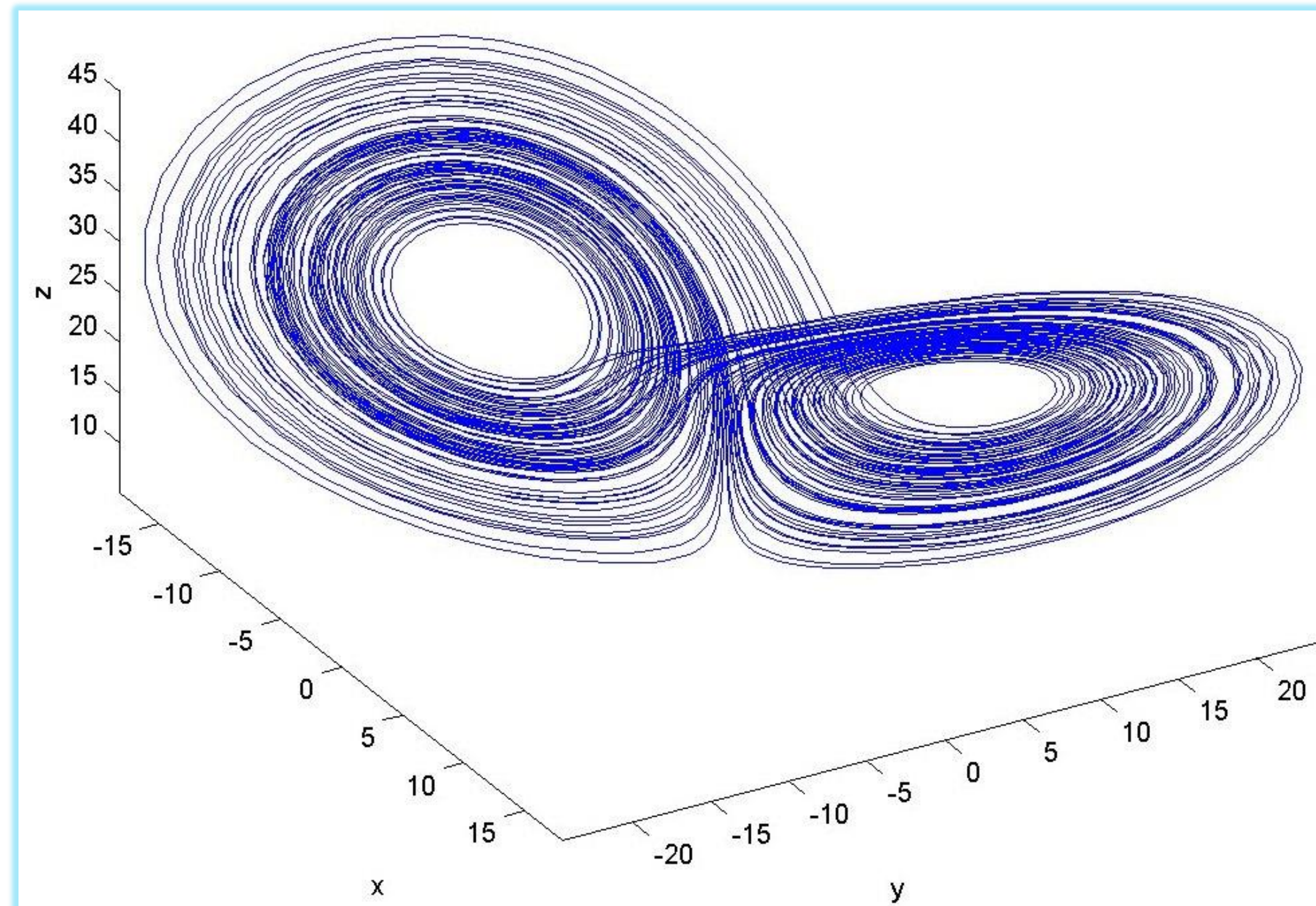


Davide Faranda<sup>1</sup>, Sandro Vaienti<sup>2</sup>  
<sup>1</sup> Laboratoire SPHYNX, Service de Physique de l'Etat Condensé, DSM, CEA Saclay, CNRS URA 2464, 91191 Gif-sur-Yvette, France  
<sup>2</sup> Aix Marseille University CNRS, CPT, UMR 7332, 13288 Marseille, France



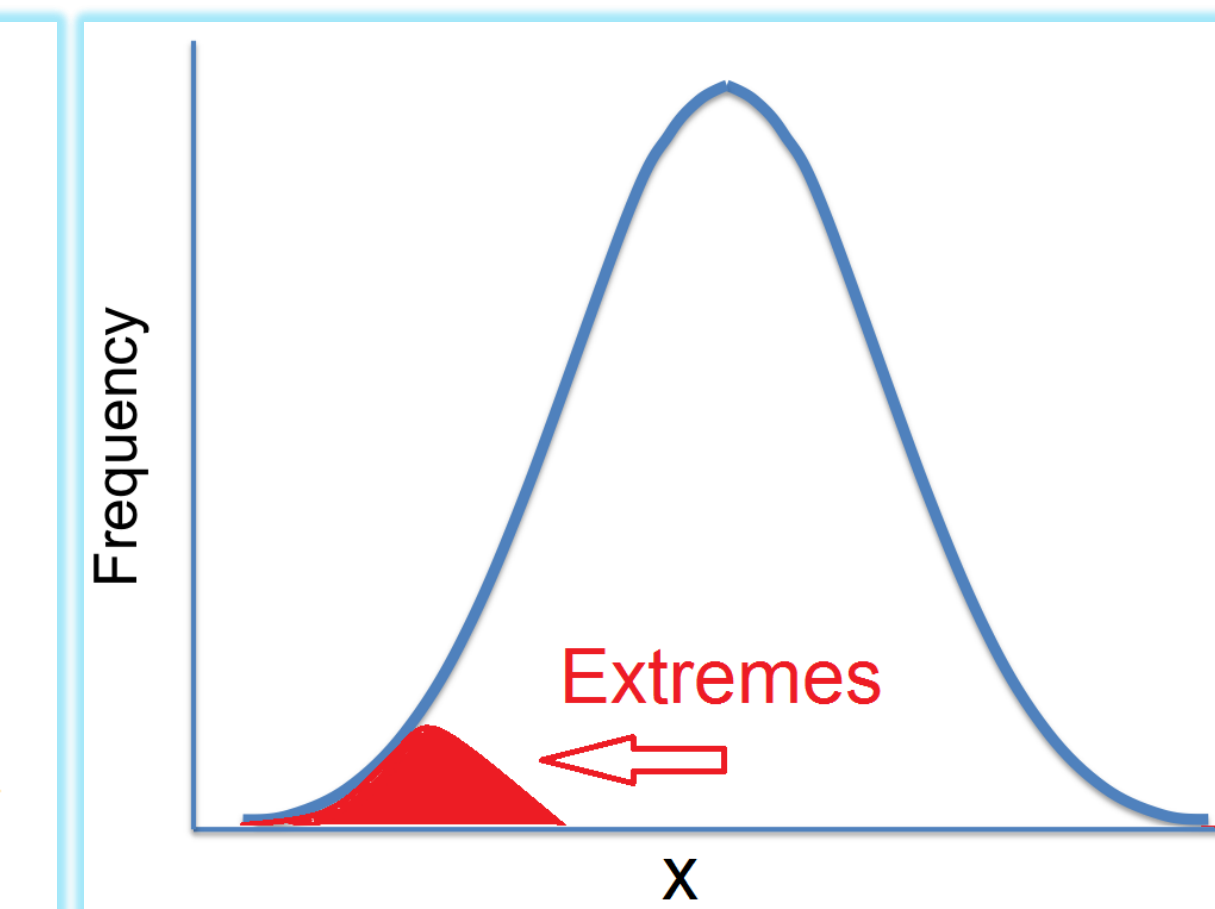
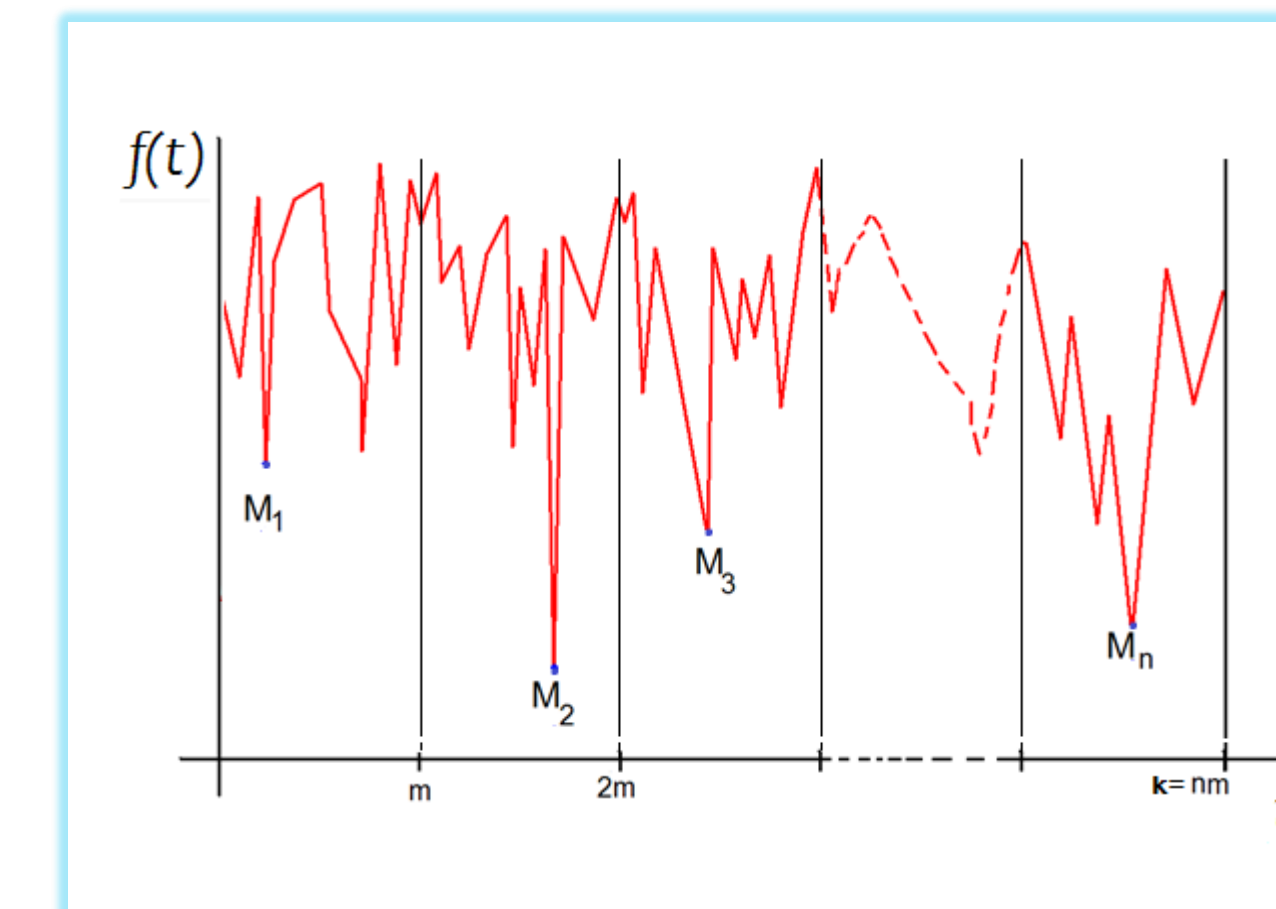
## How to define extreme events in complex systems?

### 2. Atmospheric attractors are *Strange Attractors*



When we have complex objects (as **the Lorenz strange attractors** in the figure), the Block Minima approach does not seem insightful. **Maxima or Minima of the single variables do not represent dynamical features of the attractor!**

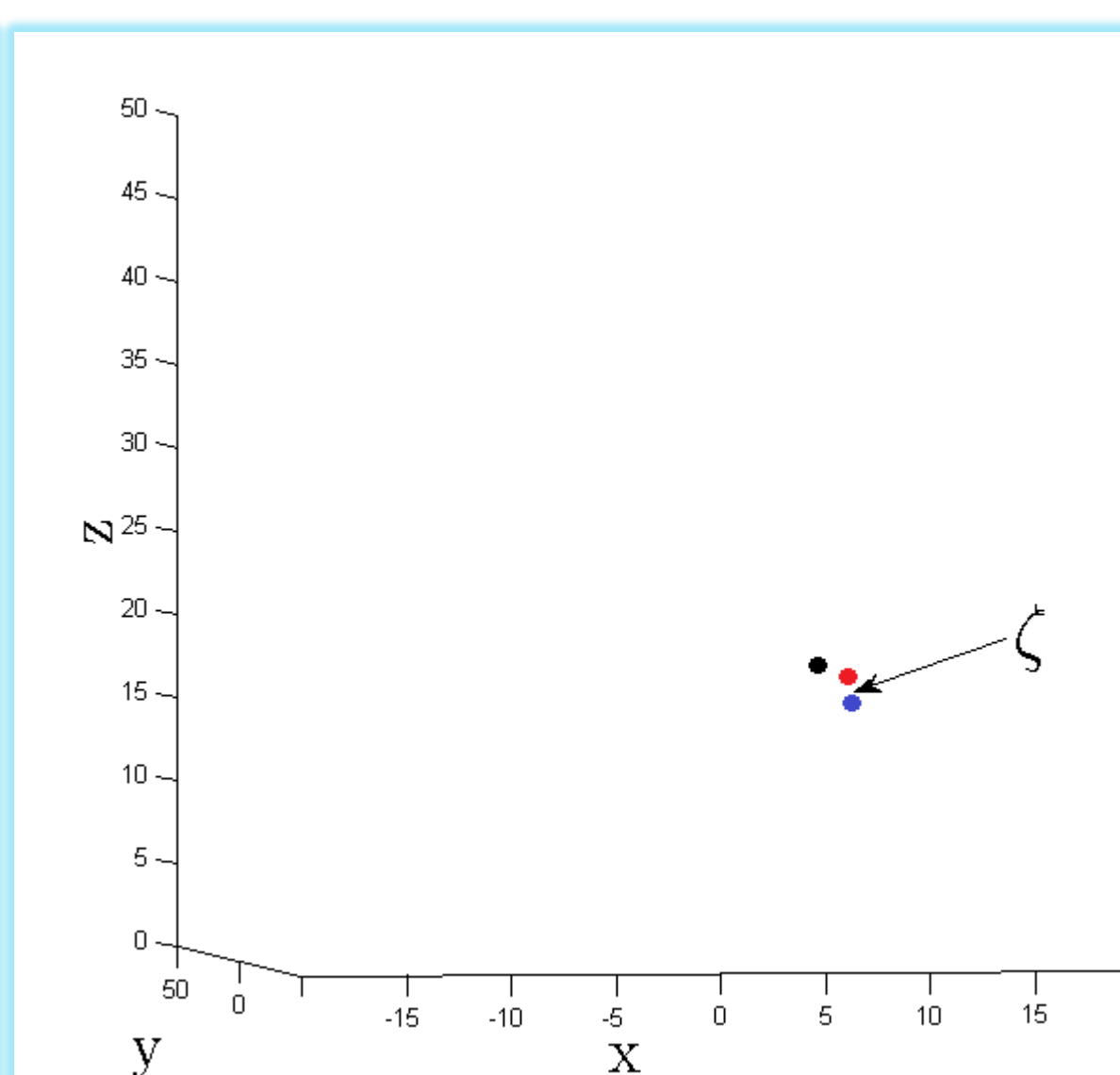
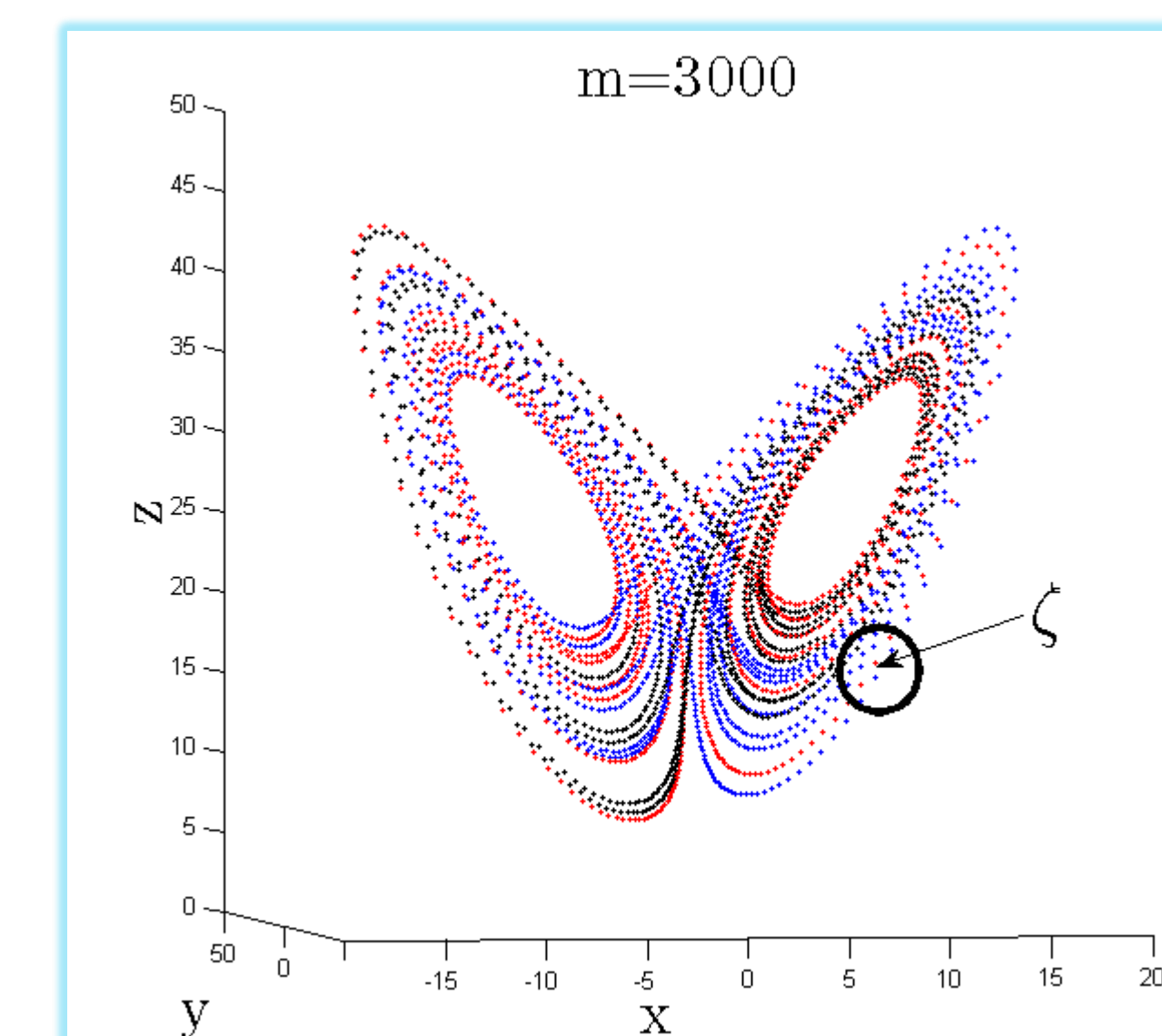
### 1. The traditional statistical approach for time series



#### Block Minima

It is the standard approach used for series of Independent and Identically distributed variables. By using the **Block Minima** approach we get **Generalized Extreme Value** distributions.

### 3. Extremes as points visited sporadically

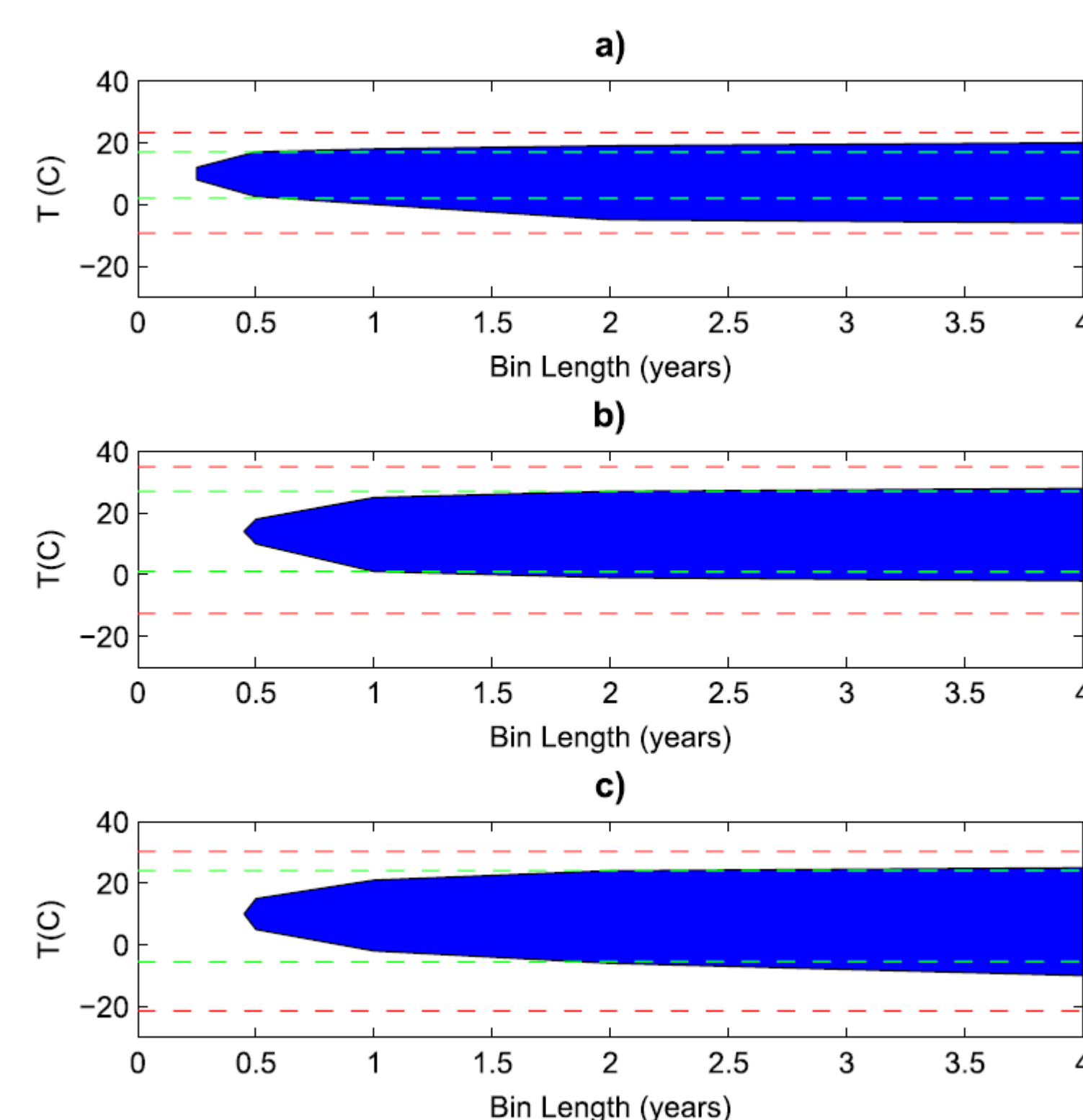


We can identify extremes of Attractors as points which are **visited rarely**. The **frequency of visit can be fixed by the Block Minima approach** as the length of the time interval in which we sample the statistics of the closest recurrences. By changing the bin length we can study the **typical interval of recurrence**.

## 4. Applications to Temperature Data

### Normal and Extremes Temperatures

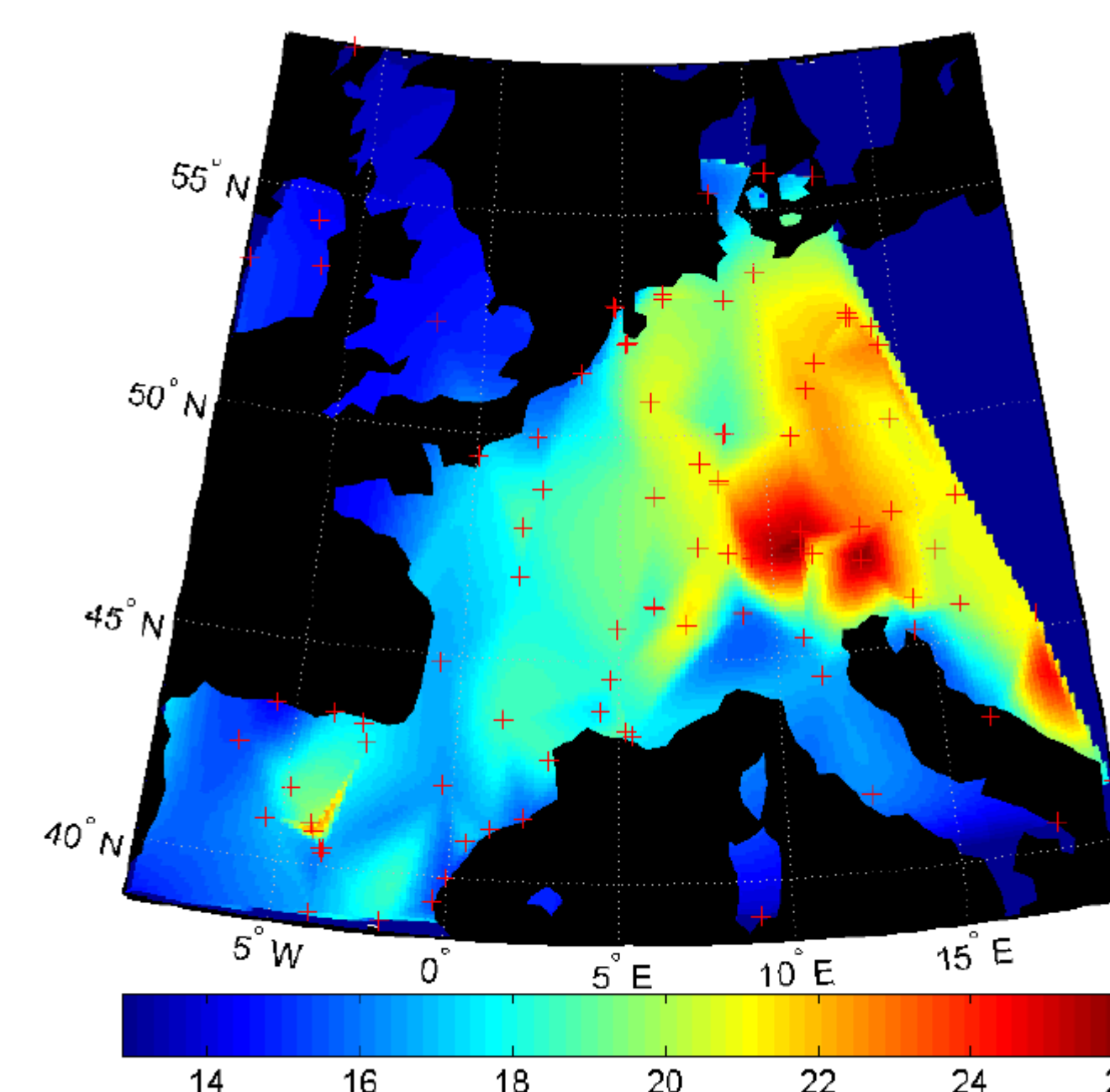
The experiments have been repeated for different bin lengths between 3 months and 4 years. In the figure, the blue area represents the reference temperatures  $\zeta$  having enough recurrences for the chosen bin length. This temperature range is what we propose as a rigorous definition of normal variability.



Region of temperatures with normal recurrences fit (blue area) for different bin lengths. Red dotted lines: absolute extremes of the temperature series for (a) Armagh, (b) Milan, and (c) Vienna. Green dotted lines: thresholds detected with the classical GPD approach.

### A map of European *Normal* Temperatures

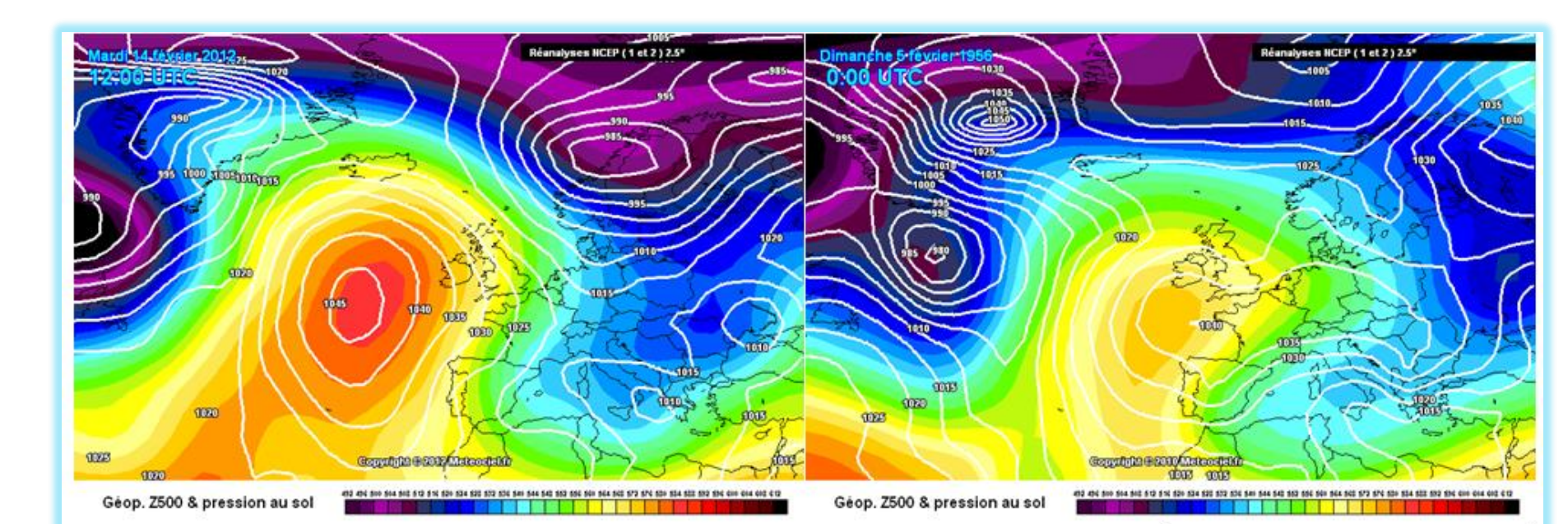
By plotting the length of the interval of convergent Temperatures at all the European locations for which at least 60 years of daily data are available, we can construct a climatological map of Europe. The results are reported in the figure for the bin length of 1 year. Different climatic regions are well highlighted.



Map of the range of *admissible temperature intervals* for the European region, obtained by considering the interval of temperature anomalies  $\zeta$  such that the fit passes the *Lilliefors* test. The red crosses represent the location of the stations used for the analysis. The straight line near the right border represents the limit of the data set.

## 5. Outlook

### A new definition of Weather Analogues



A natural extension of the method based on recurrences is to **define dynamical properties of analogues**.

A key question to answer is **whether sporadic points appear to happen more or less frequently in a climate change scenario**. Project in Collaboration with P. Yiou (LSCE – CEA SACLAY)

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